

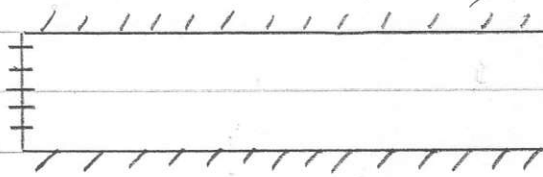
# Heat Energy flow + thermal conductivity

① A Physics 20

## 1. Patterns of heat energy flow

a) Insulated

Hot



perfect "lagging" insulation.

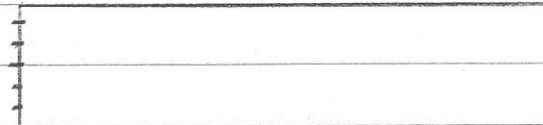
Cold

$T_H$

$T_C$

b) Un-insulated

Hot



Cold

$T_H$

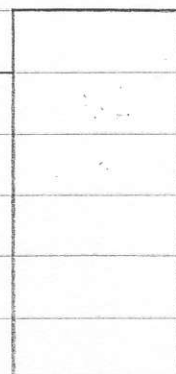
$T_C$

## 2. Calculating heat flow rates

a) Simple - single material

$Q/t =$

$22^\circ\text{C}$



brick, 10 cm thick  
 $A = 2\text{ m}^2$

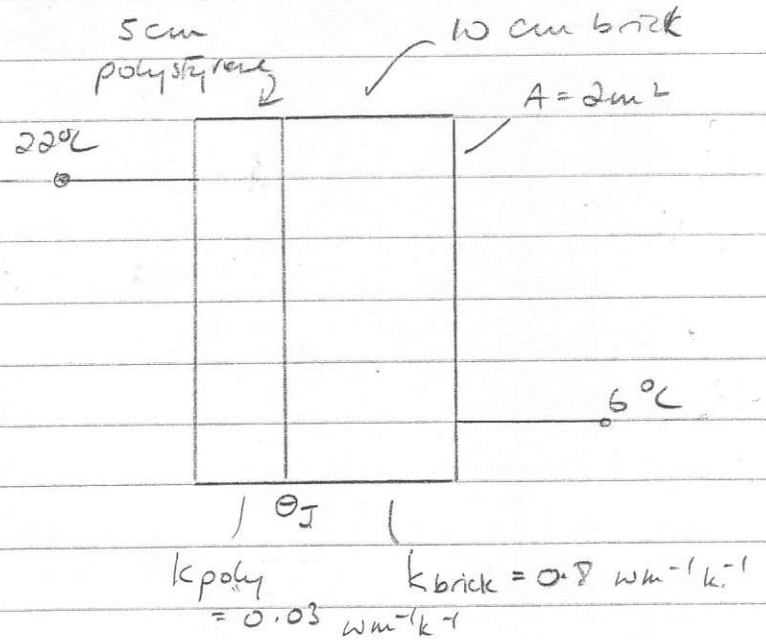
$6^\circ\text{C}$

$k_{\text{brick}} = 0.8 \text{ W/m/K}$

## Heat flow & thermal conductivity. (2)

A Physics

2(b) Advanced - two materials



3. Problems.

Calculate the rate of heat loss through  $5\text{m}^2$  of brick wall (12cm thick) with a 3cm layer of polystyrene on the inside.

4. Heat flow can be given in U-value - units  $\text{Watts}/\text{m}^2/\text{K}$ .  
What is the U value of ...

(a) the brick wall in 2(a)?

(b) the wall in 2(b)?

# Heat Energy Flow + Thermal Conductivity Answers A Physics (the hard stuff).

1 - done in class.

2. (a) Simple  $Q/t = kA \frac{\Delta\theta}{\Delta l} = 0.8 \times 2 \times \frac{16}{0.1} = 256 \text{ J/s}$

(b) Advanced

When everything is steady...

rate of heat flow through polystyrene = rate of heat flow through brick

So...  $Q/t = k_{\text{poly}} A_{\text{poly}} \frac{(22 - \theta_J)}{l_{\text{poly}}} = k_{\text{brick}} A_{\text{brick}} \frac{(\theta_J - 6)}{l_{\text{brick}}}$

$\frac{0.03 (22 - \theta_J)}{0.05} = \frac{0.8 (\theta_J - 6)}{0.1}$  Areas cancel!

$13.2 + 48 = 8.6 \theta_J$  so  $\theta_J = 7.12^\circ\text{C}$

Put back into one of the equations... say brick

$Q/t = \frac{0.8 \times 2 (7.12 - 6)}{0.1} = 17.9 \text{ J/s}$

R for brick

don't forget AREA!

3. Once more, with feeling...

$Q/t = \frac{0.03 \times A (22 - \theta_J)}{0.03} = \frac{0.8 \times A (\theta_J - 6)}{0.12}$

$\Rightarrow \theta_J = 8.08^\circ\text{C}$

bigger area

$\Rightarrow Q/t = \frac{0.03 \times 5 \times (22 - 8.08)}{0.03} = 69.6 \text{ J/s}$

4. (a) - from 2a  $Q/t = 256 \text{ J/s}$  for  $2\text{m}^2$  and  $16^\circ\text{C}$  diff

$= U \times A \times \Delta\theta$

so  $U_{\text{wall}} = \frac{256}{2 \times 16} = 8 \text{ W/m}^2\text{/K}$

(b) - from 2b  $Q/t = 18 \text{ J/s} = U \times A \times \Delta\theta$

so  $U = \frac{18}{2 \times 16} = 0.56 \text{ W/m}^2\text{/K}$