

Linear Dynamics - Force & Motion

Sheet 1/

A-Physics
Dynamics

take $g = 10 \text{ N/kg}$.

$m = 700 \text{ kg}$

$F = 250 \text{ N}$

Friction
 $= 0$



1. Level ground: no friction

A man pushes a car for 20 seconds, as shown $\rightarrow$

Calculate ... (a) acceleration 2

(b) distance moved in 20 s 2

(c) work done in 20 s. 2

(d) Hence, find the car's KE at 20 s. 2

(e) Find the man's power at 20 s. 3

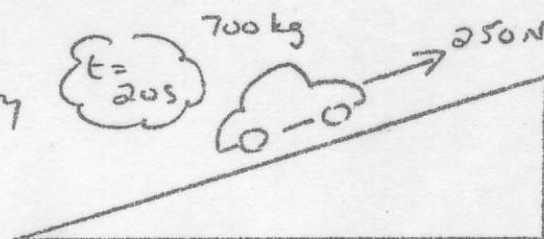
(f) The man stops pushing at $t = 20 \text{ s}$: what does the car do? Why? 2

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2. Slope - still no friction

The slope rises 1 m for every 50 m up the slope.

Otherwise - as in Q.1.



(a) Draw a labelled diagram

to show the angle of the slope, and all forces acting 4 NOT components!

(b) What is the component of weight down the slope? 2

(c) Find the resultant force on the car. 2

(d) Find the acceleration up the slope. 2

At time $t = 20 \text{ s}$, find ... (e) the car's velocity 2

(f) the man's power 2

(g) the P.E. gained by the car. 2

(h) If the man's maximum power is 300 W, what is the car's maximum speed up the slope? 2

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3. Level ground - friction acting

As in Q.1 - but constant friction force of 50 N.

(a) Draw a diagram to show all forces acting, and the resultant 4

(b) Find the car's acceleration 2

When the car has moved 50 m, calculate ...

(c) the work done against friction 2

(d) work done by the man 2

(e) the car's KE. 2

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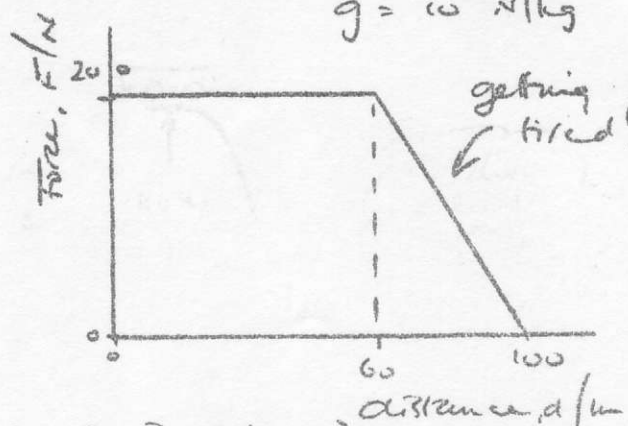
Linear Dynamics - Sheet 2/2

Continued...

A Physics Dynamics

$$g = 10 \text{ N/kg}$$

4. A man slides a block of concrete along a level road. (Some Physics teachers will do anything for a free!). The block starts + ends at rest.



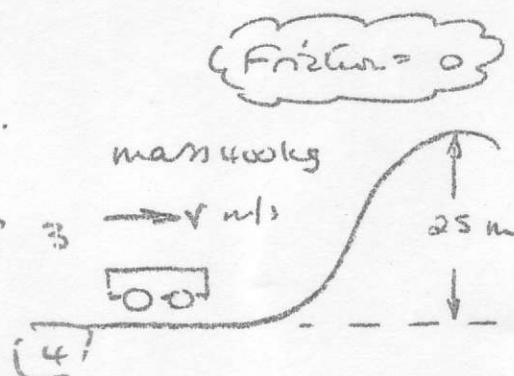
- (a) What is the work done? 3
(b) How much energy has the work produced? What kind of energy is produced? Explain clearly how this energy is produced. 5

5. Theme Park Ride...

The truck must get over the hill...

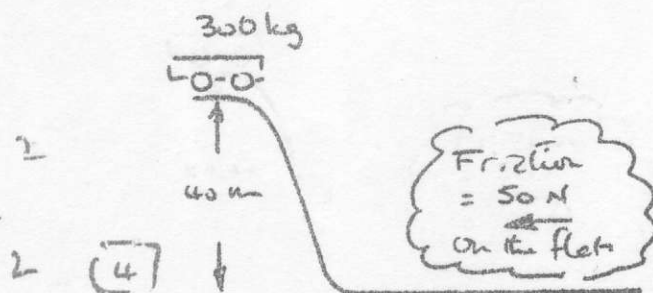
For what velocity is needed for...

- (a) the truck just to get over the hill? 3
(b) the truck to have a velocity of 5 m/s at the top? 1



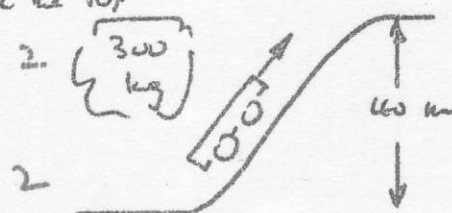
6. (a) How much P.E. does the truck start with? 2

- (b) How far does it roll on its flat before stopping? 2



7. An electric motor pulls the truck up to the top

- (a) How much energy must the truck gain? 2
(b) If the motor does this in 30 s, what is its power? 2



- (c) "The motor is 70% efficient." Explain this.

What must be the input power to the motor? 3

- (d) The motor runs off 240 V mains: what current does it need? 2

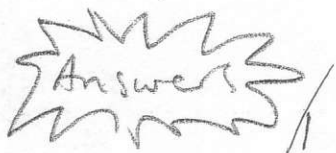
- (e) What is the major energy loss? How much is this energy produced? 3

(c) Ext. As Q. 2, but with 50 N friction. What is the maximum angle

the man can... (a) just hold the car still?
(b) just move it uphill?

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Linear Dynamics -

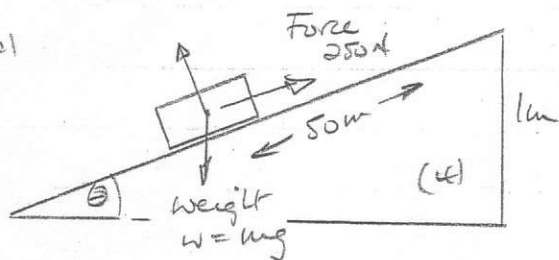


A Physics

1. (a) $a = F/m = 0.36 \text{ m/s}^2$ (2)
 (b) $s = ut + \frac{1}{2}at^2 \Rightarrow \frac{1}{2}at^2 = 71.4 \text{ m}$ (2)
 (c) Work $W = F \times d = 250 \times 71.4 = 17,860 \text{ J} = 17.9 \text{ kJ}$ (2)
 (d) Work done $\rightarrow KE$, so $KE = 17.9 \text{ kJ}$ (1)
 (e) Power = Force $\times$ distance / Time = Force $\times v$...
 $KE = \frac{1}{2}mv^2 = 17,860 \text{ J} \rightarrow v = 7.1 \text{ m/s}$
 so power $P = F \times v = 1786 \text{ Watts}$, (3) (13)
 (f) Car keeps going at the same velocity ... because no friction! (1)
 Reaction (at 90° to hill)

2.

(a)



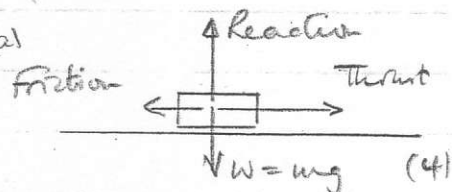
(b) Component of $W_{\text{slope}} = mg \sin \theta$
 weight
 $= 700 \times 10 \times \frac{1}{50}$
 $= 140 \text{ N}$ (2)

(c) $F_{\text{res}} = 250 - 140 = 110 \text{ N}$ (2)

- (d) $a = \frac{F_{\text{res}}}{m} = 110/700 = 0.157 = 0.16 \text{ m/s}^2$ (2)
 (e) $v = u + at = 0 + 0.157 \times 10 = 3.14 \text{ m/s}$ (2)
 (f) man's power $P = F \times v = 250 \times 3.14 = 786 \text{ Watts}$ (2)
 (g) PE gained by car = mgh gain = $mg \times (\text{distance up slope} / 50)$
 Distance up slope $s = ut + \frac{1}{2}at^2 = 0 + \frac{1}{2} \times 0.16 \times 20^2 = 31.4 \text{ m}$
 so PE gained = $700 \times 10 \times 31.4 / 50 = 4,400 \text{ J}$ (2)
 (h) $P_{\text{max}} = F \times v_{\text{max}} \rightarrow v_{\text{max}} = P/F = 300/250 = 1.2 \text{ m/s}$ (2) (18)

3.

(a)



(b) $a = F_{\text{res}}/m = 200/700 = 0.29 \text{ m/s}^2$

(c) Work $W = F_{\text{frict}} \times 50 = 2500 \text{ J}$

$F_{\text{res}} = 250 - 50 = 200 \text{ N}$

(d) work by man $W_m = 250 \times 50 = 12,500 \text{ J}$

- (e) Car's KE: $F_{\text{res}} \times d = KE = 200 \times 50 = 10,000 \text{ J}$ of KE
 or $v^2 = u^2 + 2as \rightarrow v \text{ after } 50 \text{ m} = \sqrt{2as} = 5.34 \text{ m/s}$
 so $KE = \frac{1}{2}mv^2 = 10,000 \text{ J}$

W
2.98

work done by man 12,500 J	KE of car 10,000 J
	work against friction 2,500 J

Linear Dynamics - Answers

A Physics

4 (a) work done = total of force $\times$ distance
= area under graph

$$= (200 \times 60) + (\frac{1}{2} \times 200 \times 40) = \underline{16,000 \text{ J}}$$

(b) 16,000 J of Heat energy produced - atoms in surfaces rubbing together, friction, sets the atoms vibrating, gives them thermal energy. [8]

5. (a) $KE = PE$ so $\frac{1}{2}mv^2 = mgh \rightarrow v_{min} = \underline{22.3 \text{ m/s}}$ (3)

(b) $v_{min} \text{ now} = 22.3 + 5 = \underline{27.3 \text{ m/s}}$ (4) (1)

6 (a) $PE = mgh = 300 \times 10 \times 40 = \underline{120,000 \text{ J}}$ (2)

(b) $PE \rightarrow KE \rightarrow$ work against friction = $F \times \text{distance rolled}$
so $120,000 = 50 \times d \rightarrow d = \underline{2,400 \text{ m}} = \underline{2.4 \text{ km}}$!! [4]

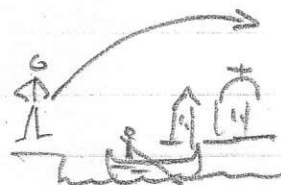
7. (a) $PE \text{ gained} = mgh = 200 \times 40 \times 10 = \underline{120,000 \text{ J}}$

(b) power $P = \text{work} / \text{time} = 120,000 / 30 = \underline{4000 \text{ W/s, W.}}$

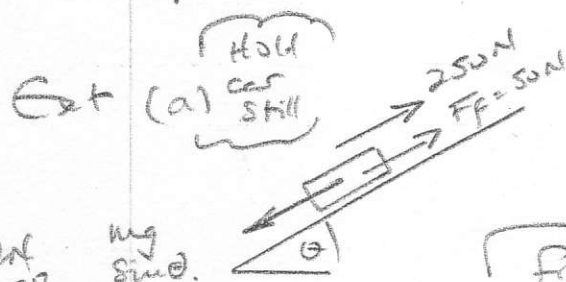
(c) 70% efficiency = for 100 J energy input - 70 J are produced
30 J are wasted

so $P_{input} = 4000 \times \frac{100}{70} = \underline{5710 \text{ W.}}$ (3)

(d) $P_{elec} = I \times V \rightarrow I = P/V = \underline{23.8 \text{ A}}$ (2)



(e) motor energy lost = 30% of input = $\frac{30}{100} \times 5710 = \underline{1700 \text{ W}}$
produced as HEAT by - elec. heating in wires
- friction between moving parts

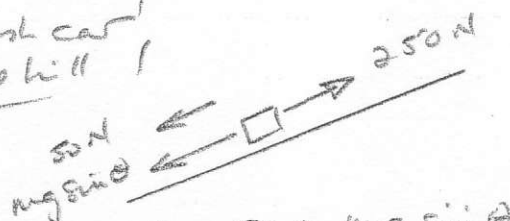


$mg \sin \theta$

$$mg \sin \theta = 250 + 50$$

$$\Rightarrow \theta_{max} = \underline{2.5^\circ}$$

(b) push car up hill



$mg \sin \theta$

$$250 = 50 + mg \sin \theta$$

$$\Rightarrow \theta_{max} = \underline{1.6^\circ}$$

friction force always opposes motion!!