

Diffraction Gratings

A Physics

1. a) What does each term in the diffraction grating equation mean? (2)
- b) A grating is marked "5500 lines/cm". What is the spacing between two adjacent slits in m? (2)
- c) Sodium street light is orange, with a frequency of 5.1×10^{14} Hz. What is the wavelength of sodium light? (2)
- d) At what angles are the 1st and 2nd order diffracted rays produced? Draw a simple diagram to show this (5)
- e) Can a 3rd order diffracted ray be produced? Explain your answer (2: even correct guess gets 0).

$$c_{\text{light}} = 3 \times 10^8 \text{ m/s}$$

$$\lambda_{\text{red}} = 700 \text{ nm}$$

$$\lambda_{\text{blue}} = 400 \text{ nm}$$

$$1 \text{ nm} = 1 \times 10^{-9} \text{ m}$$

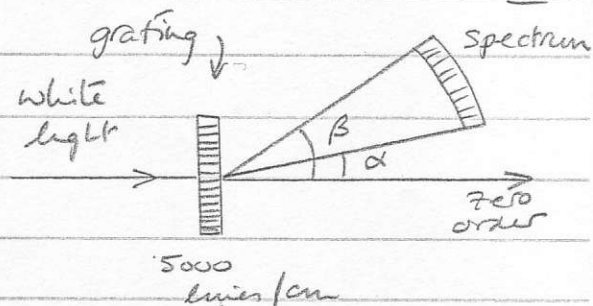
$$n \lambda = d \sin \theta$$

2. Mercury street light has 2 main colours, blue and green. The green light has a wavelength of 546 nm.

- (a) What is the spacing for a diffraction grating with 4000 lines/cm? (2)
- (b) Mercury light is shone through this grating. Calculate the angles of the 1st and 2nd order diffracted rays of the green light. (3)
- (c) The angle for the 1st order diffracted blue light is 10.0° . Calculate the frequency and wavelength of mercury blue light (4)
- (d) Draw a simple diagram showing the diffracted green and blue rays. (2)

3. When white light is shone on to a diffraction grating a spectrum is produced.

- (a) Why? (3)
- (b) Draw a simple diagram to show the spectrum. (2)
- (c) Calculate the diffraction angles of the red and blue ends of the spectrum (3)



2.99

Q... 1.../13

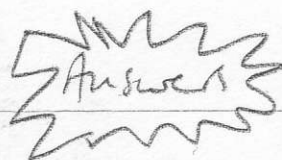
2 / 11

3/8

Total 1/32

8

Diffraction Grating



A Physics

1. a) $n\lambda = d \sin \theta$ angle of diffraction
 of order n wavelength, λ grating spacing, d ($\frac{1}{2}$ each)

b) $5500 \text{ lines/cm} = 5.5 \times 10^5 \text{ lines/m} \Rightarrow d = 1.82 \times 10^{-6} \text{ m}$ (2)

c) $v_{\text{light}} = f\lambda \Rightarrow \lambda = v/f = 3 \times 10^8 \times 5.1 \times 10^{14} = 588 \times 10^{-9} \text{ m}$ (2)

d) 1st order... $1 \times \lambda = d \sin \theta \Rightarrow \sin \theta = 0.323 \Rightarrow \theta = 18.9^\circ$ (1)

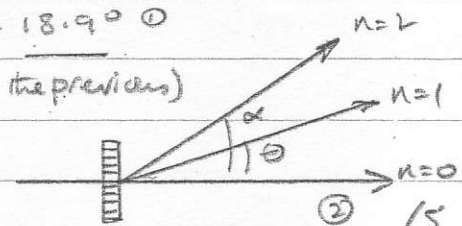
2nd order... $2 \times \lambda = d \sin \theta \Rightarrow \sin \theta = 0.646$ (2x the previous)

so $\theta = 40.3^\circ$ (1)

e) for 3rd order... $3\lambda = d \sin \theta$ (1)

so $\sin \theta = 3\lambda/d = 3 \times 588 \times 10^{-9} / 1.82 \times 10^{-6} = 0.97 \Rightarrow \theta = 75.8^\circ$ (1)

so a third order diffracted ray can be produced - yes (1) (2) 15



2. a) spacing $d = \frac{1}{4000 \times 10^3} \text{ m} = 2.5 \times 10^{-6} \text{ m}$ (2)

b) 1st order... $n\lambda = d \sin \theta \Rightarrow \sin \theta = n\lambda/d = 1 \times 546 \times 10^{-9} / 2.5 \times 10^{-6} = 0.2184$ (1)

$n\lambda = d \sin \theta \Rightarrow \sin \theta = n\lambda/d = 1 \times 546 \times 10^{-9} / 2.5 \times 10^{-6} = 0.2184$
 $\theta = 12.6^\circ$ (1)

2nd order... $\sin \theta = 2 \times 546 \times 10^{-9} / 2.5 \times 10^{-6} = 0.4368$ (1)

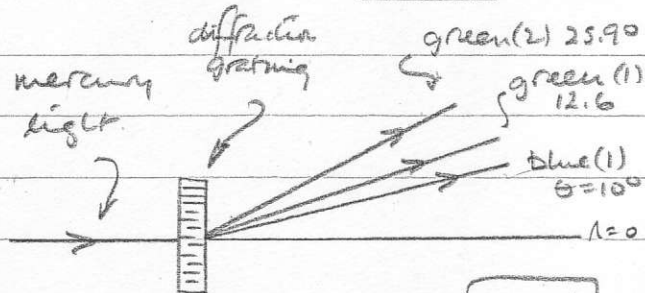
(3)

c) Blue light... $n\lambda = d \sin \theta \Rightarrow 1 \times \lambda = 2.5 \times 10^{-6} \times \sin 10 \Rightarrow \lambda = 434 \times 10^{-9} \text{ m}$ (1)

Since $v_{\text{light}} = f\lambda$, $f_{\text{blue}} = v/\lambda = 3 \times 10^8 / 434 \times 10^{-9} = 6.9 \times 10^{14} \text{ Hz}$ (4)

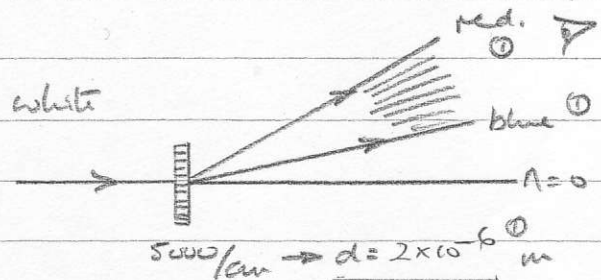
d) 4 diffracted rays... $\frac{1}{2}$ each (2)

total 11



3. a) "white" light is a combination of all the colours of the spectrum (1)

The diffraction angle depends on the wavelength. Blue, with the smallest wavelength, has the smallest angle, red the largest. - the different colours are spread into a spectrum.



(b) see diagram ...

c) red, $\lambda_{\text{red}} = 700 \text{ nm}$ $n\lambda = d \sin \theta \Rightarrow \sin \theta = \frac{\lambda}{d} = 0.35 \Rightarrow \theta = 20.5^\circ$ (1)

$\lambda_{\text{blue}} = 400 \text{ nm} \Rightarrow \sin \theta_{\text{blue}} = 0.2 \Rightarrow \theta_{\text{blue}} = 11.5^\circ$ (1)

8

FW 3.25

0...	1	2	3	total
	13	11	8	32