

WAVES - Diffraction + Interference ①

A - Physics

Formulae....

$$\frac{\lambda}{d} = \frac{s}{D} \quad \text{fringe spacing}$$

slit spacing slit-screen

data....

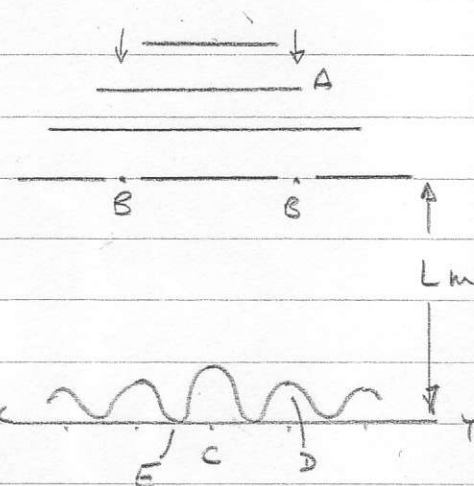
$$V_{\text{light}} = 3 \times 10^8 \text{ m/s}$$

$$V_{\text{sound (air)}} = 330 \text{ m/s}$$

1. A Science teacher is teaching diffraction and interference to his students. After a bit of trouble, he manages to make the demonstration work. In conclusion he says...

"Plane waves at A are diffracted by the narrow gaps (B). These act as two coherent sources of waves, which interfere with each other.

The detector, moving along line XY, shows the amplitude of the waves to vary as shown."



- (a) What do the underlined words mean? (5)

- (b) Explain why the amplitude is....

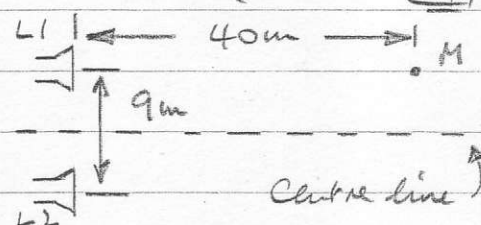
(i) large at C (3)

(ii) large at D (2)

(iii) zero at E (2)

- (c) The dimensions of the apparatus are as follows: $BB = 15 \text{ cm}$, $L = 70 \text{ cm}$, $CD = 8.0 \text{ cm}$. What are the frequency and wavelength of the microwaves? (5) 17

2. Two loudspeakers (L_1, L_2) emit sound waves in phase. As the frequency is increased from 100 - 1000 Hz, the amplitude of sound at M varies between zero and a maximum loudness.

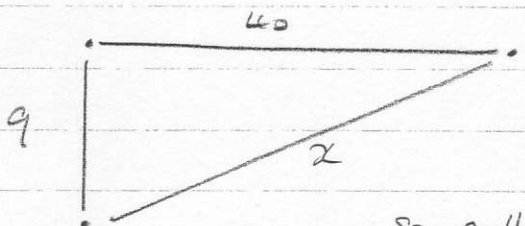


- (a) What is the path difference $L_2M - L_1M$? (2)
- (b) Explain why the amplitude varies as f is increased. (3)
- (c) The amplitude at M is zero at $f = 165 \text{ Hz}$. Explain why - use a diagram to help. (4)
- (d) There are 2 other frequencies between 100 and 1000 Hz where no sound is heard at M - what are they? (4) 9

Diffraction + Interference Answers A Physics

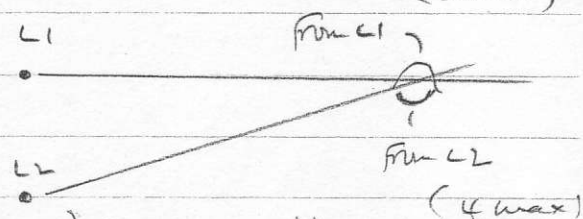
1. (a) plane - straight, from a source a long way off.
 diffracted - spreading out from a point source into gap; circular
 coherent - in step; same frequency/wavelength; constant phase
 interfere - waves pass through each other, amplitudes difference
 add up; crests add, crest cancels trough
 amplitude - "size" of wave from rest line (5)

- (b) (i) crests arrive in phase because ... path difference is zero...
 so constructive interference ... 2 crests (or 2 troughs) together 3 waves
 (ii) constructive interference ... because path difference ... = 1λ (2)
 (iii) path difference = $\frac{1}{2}\lambda$... destructive interference
 (c) Interference formula $\frac{\lambda}{d} = \frac{s}{D}$ so ... $\lambda = \frac{s \cdot d}{D} = \frac{8 \times 10^{-2} \times 15 \times 10^{-2}}{70 \times 10^{-2}} = 0.0171 \text{ m} = 1.7 \text{ cm}$
 then ... $v = f\lambda$ so $f = \frac{v}{\lambda} = \frac{3 \times 10^8 \text{ m/s}}{0.017 \text{ m}} = 1.75 \times 10^{10} \text{ Hz}$
 (to get f in Hz, you must get λ in m.) (5)
17

2. (a)  Use Pythagoras
 $x^2 = 40^2 + 9^2 = 1681$
 so $x = 41 \text{ m}$ (surprise!)
 so path difference = $41 - 40 = 1 \text{ m}$ (2)

- (b) the path difference stays constant at 1m ... but the wavelength changes as frequency increases ... so some times p.d. = λ ...
 and some times p.d. = $\lambda/2$ (3 max)

- (c) for $f = 164 \text{ Hz}$... $\lambda = \frac{v}{f} = 2.0 \text{ m}$
 so path diff = $1 \text{ m} = \lambda/2$... destructive interference



- (d) for no sound at π ... p.d. must = $\lambda/2$ or an odd multiple.
 $\text{p.d.} = 1 \text{ m} = 1 \times \lambda/2$ $\lambda = 2 \text{ m}$ $f = v/\lambda = 165 \text{ Hz}$
 $\text{p.d.} = 1 \text{ m} = 3 \times \lambda/2$ $\lambda = \frac{2}{3} \text{ m} = 0.667$ $f = 495 \text{ Hz}$
 $\text{p.d.} = 1 \text{ m} = 5 \times \lambda/2$ $\lambda = \frac{2}{5} \text{ m} = 0.4 \text{ m}$ $f = 825 \text{ Hz}$
 $\text{p.d.} = 1 \text{ m} = 7 \times \lambda/2$ $\lambda = \frac{2}{7} \text{ m} = 0.286 \text{ m}$ $f = 1155 \text{ Hz}$
 4.99
 11.99
 2. ... ① 17 ② 13. Total 126 30.
That's easy!
13